CLAIMS

What is claimed is:

1. A method for determining abnormal consumption of a utility by a system:

repeatedly measuring the level of use of the utility thereby producing a plurality of utility measurements;

employing a statistical procedure to identify any outliers in the plurality of utility measurements; and

evaluating performance of the system in response to any outliers identified.

- 2. The method as recited in claim 1 wherein evaluating performance of the system comprises determining a severity of abnormal utility usage represented by an outlier.
- 3. The method as recited in claim 2 wherein determining a severity of abnormal utility usage comprises calculating how many standard deviations a given outlier is from the average value for utility usage by using the expression:

$$z_{j} = \frac{x_{e,j} - \overline{x}_{robust}}{s_{robust}}$$

where $x_{e,j}$ is the energy consumption for the j^{th} outlier, \overline{x}_{robust} is a robust estimate of the average energy consumption for days of the same day type as outlier j, and s_{robust} is a robust estimate of the standard deviation of energy consumption for days of the same day type.

- 4. The method as recited in claim 2 wherein determining a severity of abnormal utility usage comprises calculating a standard deviation of each outlier.
- 5. The method as recited in claim 2 wherein determining a severity of abnormal utility usage comprises determining an amount that each outlier deviates from a mean of the plurality of utility measurements which are not identified as outliers.
- 6. The method as recited in claim 1 further comprising separating the plurality of utility measurements into groups wherein each group contains utility measurements acquired during days that under normal conditions have similar utility consumption levels; and

wherein the statistical procedure is applied separately to each group.

7. The method as recited in claim 1 further comprising separating the plurality of utility measurements into groups wherein each group contains utility measurements acquired during predefined time periods that under normal conditions have similar utility consumption levels; and

wherein the statistical procedure is applied separately to each group.

- 8. The method as recited in claim 1 wherein the outliers are identified using a Generalized Extreme Studentized Deviate (GESD) statistical procedure.
- 9 The method as recited in claim 8 wherein employing a statistical procedure involve utilizing a Generalized Extreme Studentized Deviate (GESD) statistical procedure comprising:
- (a) calculating an arithmetic mean $\left(\overline{x}\right)$ of the plurality of utility measurements;
- (b) finding an extreme utility measurement $x_{e,i}$ which is the utility measurement that has a value which is farther numerically from the arithmetic mean (\bar{x}) than the other ones of the plurality of utility measurements;
- (c) using the extreme utility measurement $x_{e,i}$ to calculate an extreme studentized deviate R_i ;
- (d) calculating a 100α percent critical value λ_i for the extreme utility measurement $x_{e,i}$;
- (e) declaring the extreme utility measurement $x_{e,i}$ to be an outlier when the extreme studentized deviate R_i is greater than the 100α percent critical value λ_i .

10. The method as recited in claim 9 further comprising: removing the extreme utility measurement $x_{e,i}$ from the plurality of utility measurements to form a new plurality of utility measurements; and

repeating steps (a) through (e) for the new plurality of utility measurements.

11. The method as recited in claim 9 wherein the extreme studentized deviate R_i is calculated according to the expression:

$$R_i = \frac{\left| x_{e,i} - \overline{x} \right|}{s}$$

where s is a standard deviation of the plurality of utility measurements.

12. The method as recited in claim 9 wherein the 100α percent critical value λ_i then is calculated using the equation:

$$\lambda_{i} = \frac{(n-i)t_{n-i-1,p}}{\sqrt{(n-i+1)(n-i-1+t_{n-i-1,p}^{2})}}$$

where n is the number of utility measurements, i is a number identifying a particular outlier being evaluated, $t_{n-i-1,p}$ is a student's t-distribution with (n-i-1) degrees of freedom, and p is a value based on the user defined probability α of incorrectly declaring one or more outliers when no outliers exist.

13. The method as recited in claim 12 wherein percentile p is determined from:

$$p=1-\left(\frac{\alpha}{2(n-i+1)}\right).$$

- 14. A method for determining abnormal consumption of a utility by a system:
- (a) repeatedly measuring the level of use of the utility, thereby producing a plurality of utility measurements;
- (b) forming a group of those of the plurality of utility measurements taken during predefined periods of time;
 - (c) calculating an arithmetic mean $(ar{x})$ of the group;
- (d) finding an extreme utility measurement $x_{e,i}$ which is the utility measurement having a value that is farthest numerically from the arithmetic mean (\bar{x}) ;
- (e) using the extreme utility measurement $x_{e,i}$ to calculate an extreme studentized deviate $R_{\scriptscriptstyle 2}$;
- (f) calculating a 100α percent critical value λ_i for the extreme utility measurement $x_{e,i}$;
- (g) declaring the extreme utility measurement $x_{e,i}$ to be an outlier indicative of abnormal utility use when the extreme studentized deviate is greater than the 100α percent critical value;

- (h) removing the extreme utility measurement $x_{e,i}$ from the group of utility measurements; and
- (i) repeating steps (c) through (h) a defined number of times.
- 15. The method as recited in claim 14 wherein the extreme studentized deviate R_i is calculated according to the expression:

$$R_i = \frac{\left| x_{e,i} - \overline{x} \right|}{s}$$

where s is a standard deviation of the plurality of the group of utility measurements.

16. The method as recited in claim 14 wherein the 100α percent critical value λ_i is calculated using the equation:

$$\lambda_{i} = \frac{(n-i)t_{n-i-1,p}}{\sqrt{(n-i+1)(n-i-1+t_{n-i-1,p}^{2})}}$$

where n is the number of utility measurements, i is a number identifying a particular outlier being evaluated, $t_{n-i-1,p}$ is the student's t-distribution with (n-i-1) degrees of freedom, and p is a value based on the user defined probability α of incorrectly declaring one or more outliers when no outliers exist.

17. The method as recited in claim 16 wherein percentile p is determined from:

$$p=1-\frac{\alpha}{2\left(n-i+1\right)} \ .$$

- 18. The method as recited in claim 14 further comprising defining periods of time during a plurality of days in which under normal conditions similar utility consumption levels occur during each one of those periods of time.
- 19. The method as recited in claim 14 further comprising performing maintenance on the system in response to examination of one or more of the outliers.